

Question 1

In an A.P., if the sum of first X terms is Y and the sum of first Y terms is X then what will be sum of (X+Y) terms?

- a)  $2(X+Y)$  b)  $(X+Y)$  c)  $-(X+Y)$  d)  $-(2X+Y)$

Answer : c)  $-(X+Y)$ .

Solution :

We know that, sum of first n-terms of an A.P. with first term a and common difference d is  $S(n) = \frac{n}{2} (2a+(n-1)d)$ .

Given that, sum of first X terms = Y

$$\text{i.e., } S(X) = \frac{X}{2} (2a + (X-1)d) = Y$$

$$X(2a + (X-1)d) = 2Y \dots (1)$$

And, sum of first Y terms = X

$$\text{i.e., } S(Y) = \frac{Y}{2} (2a + (Y-1)d) = X$$

$$Y(2a + (Y-1)d) = 2X \dots (2)$$

Subtracting, (1) and (2), we get,

$$2X - 2Y = Y(2a + (Y-1)d) - X(2a + (X-1)d)$$

$$2X - 2Y = Y2a + Y(Y-1)d - X2a - X(X-1)d$$

$$2(X - Y) = (Y - X)(2a) + (dY^2) - Yd - (dX^2) + Xd$$

$$-2(Y - X) = (Y - X) (2a) - (Y-X)d - d(X^2 - Y^2)$$

$$-2(Y - X) = (Y - X) (2a - d) - d(X^2 - Y^2)$$

$$-2(Y - X) = (Y - X) (2a - d) - d(X-Y)(X+Y)$$

$$-2(Y - X) = (Y - X) (2a - d) + d(Y-X)(X+Y)$$

$$-2 = (2a-d) + d(X+Y)$$

$$-2 = 2a + d(X+Y-1) \dots (3)$$

We have to find the sum of X+Y terms.

$$\text{i.e., } S(X+Y) = \left[ \frac{(X+Y)}{2} \right] \times (2a + (X+Y-1)d)$$

Sub. eqn (3) in above eqn, we have,

$$S(X+Y) = \left[ \frac{(X + Y)}{2} \right] \times (-2) = -(X + Y)$$

Hence, the required answer is  $-(X + Y)$ .

Question 2

In an A.P., if the sum of first X terms is  $Z(X^2)$ , the sum of first Y terms is  $Z(Y^2)$  and X is not equal to Y, then which of the following equals the sum of first Z terms of the A.P.?

- a)  $Z^3$  b)  $(X + Y)Z^2$  c)  $(X - Y)Z^2$  d)  $Z^2$

Answer : a)  $Z^2$ .

Solution :

Given that, sum of first X terms = Z(X<sup>2</sup>)

$$\text{i.e., } S(X) = X/2 (2a + (X-1)d) = Z(X^2)$$

$$(2a + (X-1)d) = 2XZ$$

$$2a + Xd - d = 2XZ \dots (1)$$

And, sum of first Y terms = Z(Y<sup>2</sup>)

$$\text{i.e., } S(Y) = Y/2 (2a + (Y-1)d) = Z(Y^2)$$

$$(2a + (Y-1)d) = 2ZY$$

$$2a + Yd - d = 2ZY \dots (2)$$

Subtracting (1) and (2), we get,

$$Xd - Yd = 2XZ - 2ZY$$

$$(X - Y)d = 2(X - Y)Z$$

$$d = 2Z \dots (3)$$

Sub. d value in eqn (1), we have

$$(2a + (X - 1)2Z) = 2XZ$$

$$2a + 2XZ - 2Z = 2XZ$$

$$2a = 2Z$$

$$a = Z \dots (4)$$

We have to find the sum of first Z terms, i.e.,  $S(Z) = Z/2 (2a + (Z-1)d)$ .

Substitute a and d values in above eqn,

$$S(Z) = Z/2 (2Z + (Z-1) 2Z) = Z(Z + (Z-1)Z) = Z^2 + Z^3 - Z^2 = Z^3.$$

### Question 3

If S<sub>1</sub>, S<sub>2</sub> and S<sub>3</sub> are sums of first n terms of three A.P.'s with common difference 1, 2, and 3 respectively and the first term of each A.P. is 1, then which of the following relation is true?

(i)  $S_3 - S_1 = n(n+1)$

(ii)  $2(S_1 + S_2) = n(3n-1)$

(iii)  $S_1 + S_3 = 2n^2$

a) (i)&(ii) only b) (ii)&(iii) only c) (iii) only d) (i),(ii)&(iii).

Answer : c) (iii) only

Solution :

Given that, the first term of each A.P. is 1 and the common difference are 1, 2 and 3.

Since S<sub>1</sub> is the sum of first n terms of the first A.P.,  $S_1 = n/2 (2a + (n-1)d) = n/2 (2 \times 1 + (n-1)1)$

$$S_1 = n/2 (2 + (n-1)1)$$

$$S_1 = n/2 (n+1) \dots (1)$$

Since S<sub>2</sub> is the sum of first n terms of the second A.P.,  $S_2 = n/2 (2a + (n-1)d) = n/2 (2 \times 1 + (n-1)2)$

$$S_2 = n/2 (2 + (n-1)2) = n/2 (2n)$$

$$S_2 = n^2 \dots (2)$$

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Since  $S_3$  is the sum of first  $n$  terms of the third A.P.,  $S_3 = n/2 (2a + (n-1)d) = n/2 (2x_1 + (n-1)3)$

$$S_3 = n/2 (3n-1) \dots (3)$$

Now, we have to find the given relations  $S_3 - S_1$ ,  $2(S_1 + S_2)$  and  $S_1 + S_3$ .

$$S_3 - S_1 = n/2 (3n-1) - n/2 (n+1)$$

$$= n/2 [3n - 1 - n - 1]$$

$$= n/2 (2n-2) = n(n-1)$$

Therefore, (i) is not true.

$$S_1 + S_2 = n/2 (n+1) + n^2 = [n (n+1) + 2n^2]/2 = n(3n+1)/2$$

$$2(S_1 + S_2) = n (3n + 1)$$

Therefore, (ii) is not true.

$$S_1 + S_3 = n/2 (3n-1) + n/2 (n+1) = n/2 (3n - 1 + n + 1) = 2n^2$$

Therefore, (iii) is true.

Hence, the answer is option c.